

B priedas. Automobilio su slydimo sistema matematinio modelio apibendrintųjų jėgų vektoriaus nariai

Masių ir inercijos matricos:

$$[M_{auto}] = m_{auto} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}, \quad (\text{P.B.1})$$

$$[I_{auto}] = \begin{bmatrix} I_x & 0 & 0 \\ 0 & I_y & 0 \\ 0 & 0 & I_z \end{bmatrix}, \quad (\text{P.B.2})$$

$$[M_{auto,z}] = \begin{bmatrix} m_1 & 0 & 0 & 0 \\ 0 & m_2 & 0 & 0 \\ 0 & 0 & m_3 & 0 \\ 0 & 0 & 0 & m_4 \end{bmatrix}, \quad (\text{P.B.3})$$

$$[I_{auto,z}] = \begin{bmatrix} I_{y_1} & 0 & 0 & 0 \\ 0 & I_{y_2} & 0 & 0 \\ 0 & 0 & I_{y_3} & 0 \\ 0 & 0 & 0 & I_{y_4} \end{bmatrix}, \quad (\text{P.B.4})$$

$$[I_{ASS,w}] = \begin{bmatrix} I_{y_{11}} & 0 & 0 & 0 \\ 0 & I_{y_{22}} & 0 & 0 \\ 0 & 0 & I_{y_{33}} & 0 \\ 0 & 0 & 0 & I_{y_{44}} \end{bmatrix}, \quad (\text{P.B.5})$$

$$[I_{ASS,\delta}] = \begin{bmatrix} I_{z_{11}} & 0 & 0 & 0 \\ 0 & I_{z_{22}} & 0 & 0 \\ 0 & 0 & I_{z_{33}} & 0 \\ 0 & 0 & 0 & I_{z_{44}} \end{bmatrix}, \quad (\text{P.B.6})$$

Jėgų ir momentų vektoriai:

$$\{F_{auto}(X)\} = \left\{ \begin{array}{l} F_{x_1} \cos \delta_1 - F_{y_1} \sin \delta_1 + F_{x_2} \cos \delta_2 - F_{y_2} \sin \delta_2 \\ + F_{x_3} + F_{x_4} - F_{pasipr.} \\ \\ F_{x_1} \sin \delta_1 + F_{y_1} \cos \delta_1 + F_{x_2} \sin \delta_2 + F_{y_2} \cos \delta_2 \\ + F_{y_3} + F_{y_4} \\ \\ -c_1(\dot{z} - \dot{z}_1 + a_1\dot{\varphi} - b_1\dot{\theta}) - c_2(\dot{z} - \dot{z}_2 - a_2\dot{\varphi} - b_1\dot{\theta}) \\ -c_3(\dot{z} - \dot{z}_3 + a_1\dot{\varphi} + b_2\dot{\theta}) - c_4(\dot{z} - \dot{z}_4 - a_2\dot{\varphi} + b_2\dot{\theta}) \\ -k_1(z - z_1 + a_1\varphi - b_1\theta) - k_2(z - z_2 - a_2\varphi - b_1\theta) \\ -k_3(z - z_3 + a_1\varphi + b_2\theta) - k_4(z - z_4 - a_2\varphi + b_2\theta) \\ -c_{t11}(\dot{z} - \dot{z}_{011} + a_{11}\dot{\varphi} - b_{11}\dot{\theta}) - c_{t22}(\dot{z} - \dot{z}_{022} - a_{22}\dot{\varphi} - b_{11}\dot{\theta}) \\ -c_{t33}(\dot{z} - \dot{z}_{033} + a_{11}\dot{\varphi} + b_{22}\dot{\theta}) - c_{t44}(\dot{z} - \dot{z}_{044} - a_{22}\dot{\varphi} + b_{22}\dot{\theta}) \\ -k_{t11}(z - (z_{011} + \Delta z_{11}) + a_{11}\varphi - b_{11}\theta) \\ -k_{t22}(z - (z_{022} + \Delta z_{22}) - a_{22}\varphi - b_{11}\theta) \\ -k_{t33}(z - (z_{033} + \Delta z_{33}) + a_{11}\varphi + b_{22}\theta) \\ -k_{t44}(z - (z_{044} + \Delta z_{44}) - a_{22}\varphi + b_{22}\theta) \end{array} \right\}, \quad (\text{P.B.7})$$

$$\{M_{auto}(X)\} = \left\{ \begin{array}{c} Z \\ \Phi \\ \Theta \end{array} \right\}, \quad (\text{P.B.8})$$

čia:

$$\{Z\} = \left\{ \begin{array}{l} -c_1 a_1 (\dot{z} - \dot{z}_1 + a_1 \dot{\varphi} - b_1 \dot{\theta}) + c_2 a_2 (\dot{z} - \dot{z}_2 - a_2 \dot{\varphi} - b_1 \dot{\theta}) \\ -c_3 a_1 (\dot{z} - \dot{z}_3 + a_1 \dot{\varphi} + b_2 \dot{\theta}) + c_4 a_2 (\dot{z} - \dot{z}_4 - a_2 \dot{\varphi} + b_2 \dot{\theta}) \\ -k_1 a_1 (z - z_1 + a_1 \varphi - b_1 \theta) + k_2 a_2 (z - z_2 - a_2 \varphi - b_1 \theta) \\ -k_3 a_1 (z - z_3 + a_1 \varphi + b_2 \theta) + k_4 a_2 (z - z_4 - a_2 \varphi + b_2 \theta) \\ -c_{i11} a_{11} (\dot{z} - \dot{z}_{011} + a_{11} \dot{\varphi} - b_{11} \dot{\theta}) + c_{i22} a_{22} (\dot{z} - \dot{z}_{022} - a_{22} \dot{\varphi} - b_{11} \dot{\theta}) \\ -c_{i33} a_{11} (\dot{z} - \dot{z}_{033} + a_{11} \dot{\varphi} + b_{22} \dot{\theta}) + c_{i44} a_{22} (\dot{z} - \dot{z}_{044} - a_{22} \dot{\varphi} + b_{22} \dot{\theta}) \\ -k_{i11} a_{11} (z - (z_{011} + \Delta z_{11}) + a_{11} \varphi - b_{11} \theta) \\ +k_{i22} a_{22} (z - (z_{022} + \Delta z_{22}) - a_{22} \varphi - b_{11} \theta) \\ -k_{i33} a_{11} (z - (z_{033} + \Delta z_{33}) + a_{11} \varphi + b_{22} \theta) \\ +k_{i44} a_{22} (z - (z_{044} + \Delta z_{44}) - a_{22} \varphi + b_{22} \theta) \\ -m a_y \cdot h_\varphi \cdot \cos \varphi + m g \cdot h_\varphi \cdot \sin \varphi \end{array} \right\}, \quad (\text{P.B.9})$$

$$\{\Phi\} = \left\{ \begin{array}{l} c_1 b_1 (\dot{z} - \dot{z}_1 + a_1 \dot{\varphi} - b_1 \dot{\theta}) + c_2 b_1 (\dot{z} - \dot{z}_2 - a_2 \dot{\varphi} - b_1 \dot{\theta}) \\ -c_3 b_2 (\dot{z} - \dot{z}_3 + a_1 \dot{\varphi} + b_2 \dot{\theta}) - c_4 b_2 (\dot{z} - \dot{z}_4 - a_2 \dot{\varphi} + b_2 \dot{\theta}) \\ +k_1 b_1 (z - z_1 + a_1 \varphi - b_1 \theta) + k_2 b_1 (z - z_2 - a_2 \varphi - b_1 \theta) \\ -k_3 b_2 (z - z_3 + a_1 \varphi + b_2 \theta) - k_4 b_2 (z - z_4 - a_2 \varphi + b_2 \theta) \\ +c_{i11} b_{11} (\dot{z} - \dot{z}_{011} + a_{11} \dot{\varphi} - b_{11} \dot{\theta}) + c_{i22} b_{11} (\dot{z} - \dot{z}_{022} - a_{22} \dot{\varphi} - b_{11} \dot{\theta}) \\ -c_{i33} b_{22} (\dot{z} - \dot{z}_{033} + a_{11} \dot{\varphi} + b_{22} \dot{\theta}) - c_{i44} b_{22} (\dot{z} - \dot{z}_{044} - a_{22} \dot{\varphi} + b_{22} \dot{\theta}) \\ +k_{i11} b_{11} (z - (z_{011} + \Delta z_{11}) + a_{11} \varphi - b_{11} \theta) \\ +k_{i22} b_{11} (z - (z_{022} + \Delta z_{22}) - a_{22} \varphi - b_{11} \theta) \\ -k_{i33} b_{22} (z - (z_{033} + \Delta z_{33}) + a_{11} \varphi + b_{22} \theta) \\ -k_{i44} b_{22} (z - (z_{044} + \Delta z_{44}) - a_{22} \varphi + b_{22} \theta) \\ -m a_x \cdot h_\theta \cdot \cos \theta - m g \cdot h_\theta \cdot \sin \theta \end{array} \right\}, \quad (\text{P.B.10})$$

$$\{\Theta\} = \left\{ \begin{array}{l} (F_{x_1} \sin \delta_1 + F_{y_1} \cos \delta_1 + F_{x_2} \sin \delta_2 + F_{y_2} \cos \delta_2) b_1 \\ - (F_{y_3} + F_{y_4}) b_2 - (F_{x_1} \cos \delta_1 - F_{y_1} \sin \delta_1) a_1 \\ + (F_{x_2} \cos \delta_2 - F_{y_2} \sin \delta_2) a_2 - F_{x_3} a_1 + F_{x_4} a_2 + \sum_{i=1}^4 M_{z_i} \end{array} \right\}. \quad (\text{P.B.11})$$

$$\{F_{auto,z}(X)\} = \left\{ \begin{array}{l} c_1(\dot{z} - \dot{z}_1 + a_1\dot{\varphi} - b_1\dot{\theta}) + k_1(z - z_1 + a_1\varphi - b_1\theta) \\ -c_{t1}(\dot{z}_1 - \dot{z}_{01}) - k_{t1}(z_1 - z_{01}) \\ \\ c_2(\dot{z} - \dot{z}_2 - a_2\dot{\varphi} - b_1\dot{\theta}) + k_2(z - z_2 - a_2\varphi - b_1\theta) \\ -c_{t2}(\dot{z}_2 - \dot{z}_{02}) - k_{t2}(z_2 - z_{02}) \\ \\ c_3(\dot{z} - \dot{z}_3 + a_1\dot{\varphi} + b_2\dot{\theta}) + k_3(z - z_3 + a_1\varphi + b_2\theta) \\ -c_{t3}(\dot{z}_3 - \dot{z}_{03}) - k_{t3}(z_3 - z_{03}) \\ \\ c_4(\dot{z} - \dot{z}_4 - a_2\dot{\varphi} + b_2\dot{\theta}) + k_4(z - z_4 - a_2\varphi + b_2\theta) \\ -c_{t4}(\dot{z}_4 - \dot{z}_{04}) - k_{t4}(z_4 - z_{04}) \end{array} \right\}, \quad (\text{P.B.11})$$

$$\{M_{auto,w}(X)\} = \left\{ \begin{array}{l} T_{v1}i_{tr}.\eta_{tr} - T_{st,1} - F_{x1}r_{d1} - F_{ried,1}r_{d1} \\ T_{v2}i_{tr}.\eta_{tr} - T_{st,2} - F_{x2}r_{d2} - F_{ried,2}r_{d2} \\ -T_{st,3} - F_{x3}r_{d3} - F_{ried,3}r_{d3} \\ -T_{st,4} - F_{x4}r_{d4} - F_{ried,4}r_{d4} \end{array} \right\}, \quad (\text{P.B.12})$$

$$\{M_{ASS,w}(X)\} = \left\{ \begin{array}{l} -F_{x11}r_{d11} - F_{ried,11}r_{d11} \\ -F_{x22}r_{d22} - F_{ried,22}r_{d22} \\ -F_{x33}r_{d33} - F_{ried,33}r_{d33} \\ -F_{x44}r_{d44} - F_{ried,44}r_{d44} \end{array} \right\}, \quad (\text{P.B.13})$$

$$\{M_{ASS,\delta}(X)\} = \left\{ \begin{array}{l} F_{y11}d - M_{z11} \\ F_{y22}d - M_{z22} \\ F_{y33}d - M_{z33} \\ F_{y44}d - M_{z44} \end{array} \right\}. \quad (\text{P.B.14})$$